

Optimal Sampling

Determining the 'Best' Time to
Collect Samples

Objectives

- Understand the Idea of Optimal Sampling
- Understand the Graphical, Numerical and Analytical Methods of Determining Optimal Sampling Times

Why Optimal Sampling

- Samples Scarce
 - Needle stick - pain
 - Indwelling cannula - Patient sick
 - Blood loss
- Assay
 - Cost
 - Time required
- With Limited Data **we want** the Best Estimates of Parameter Values

Optimal Sampling

- Gives a Single Time per Parameter
 - Based on Known Model and Parameter Values
e.g. $k_{el} = 0.2 \text{ hr}^{-1}$ use $t = 5 \text{ hr}$
[IV Bolus - One compartment]
- Use a Range of Parameter Values
 - When Values not Exact Use a Range of Sample Times -
Choose Extreme of Range for More Points
e.g. $k_{el} = 0.1 - 0.3 \text{ hr}^{-1}$ use $t = 10$ and 3.3 hr
as well as 5 hr
[IV Bolus - One compartment]

Optimal Sampling

- How did I get the time values in the previous slide
- A number of approaches
 - Graphical
 - Analytical
 - Numerical

Graphical Approach

- One Compartment Model - IV Bolus

$$C_p = \frac{Dose}{V} \cdot e^{-kel \cdot t}$$

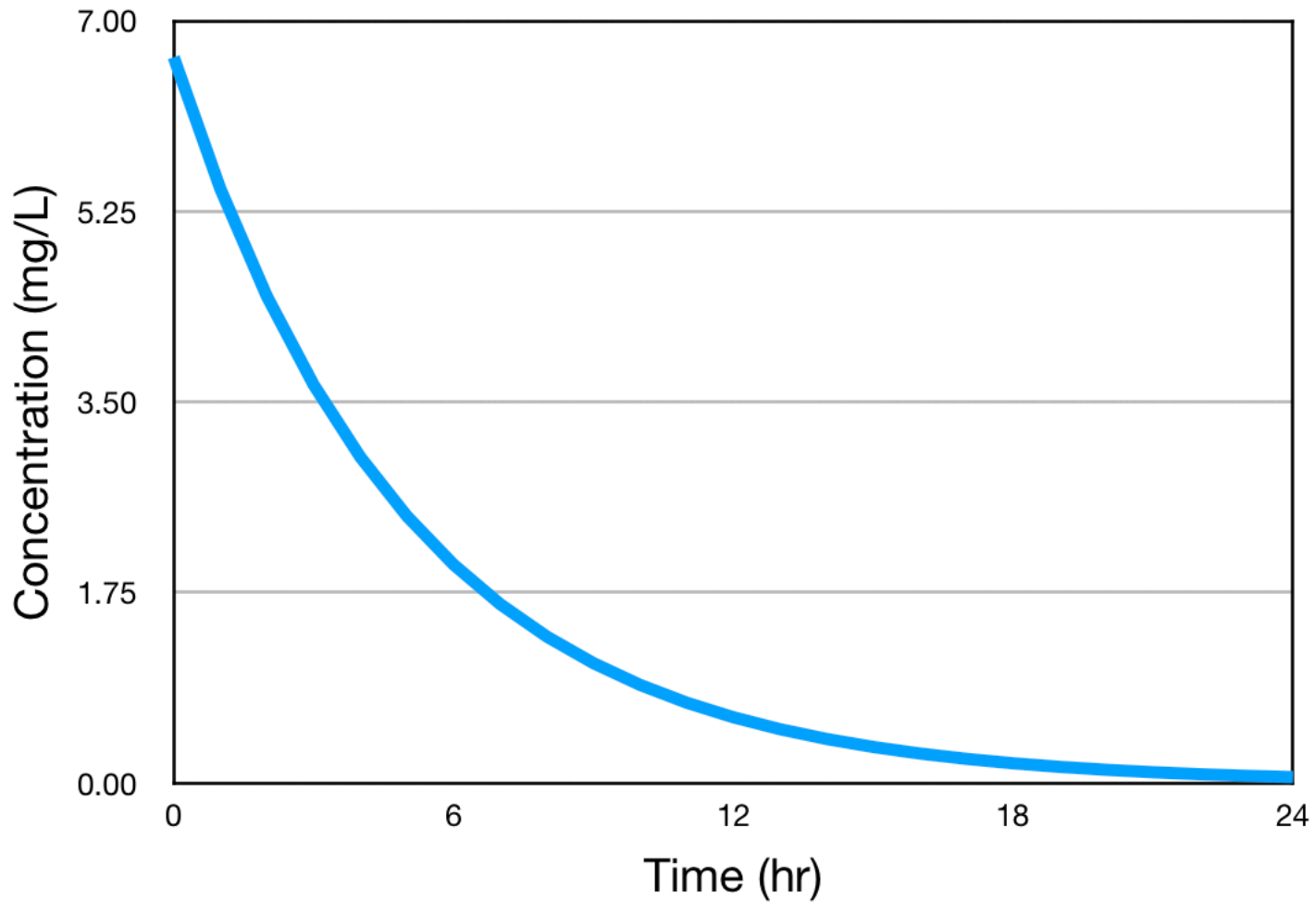
- Time for Best Values for kel and V

Graphical Approach

- Simulate Data using Known Model and Model Parameters
- Adjust One Parameters (at a time) by a Small Amount ($\pm 1, 5, 10\%$) in Both Directions
- Plot ($\Delta C_p / \Delta \text{Parameter}$) versus Time to Determine Time of Maximum Change, Maximum Sensitivity

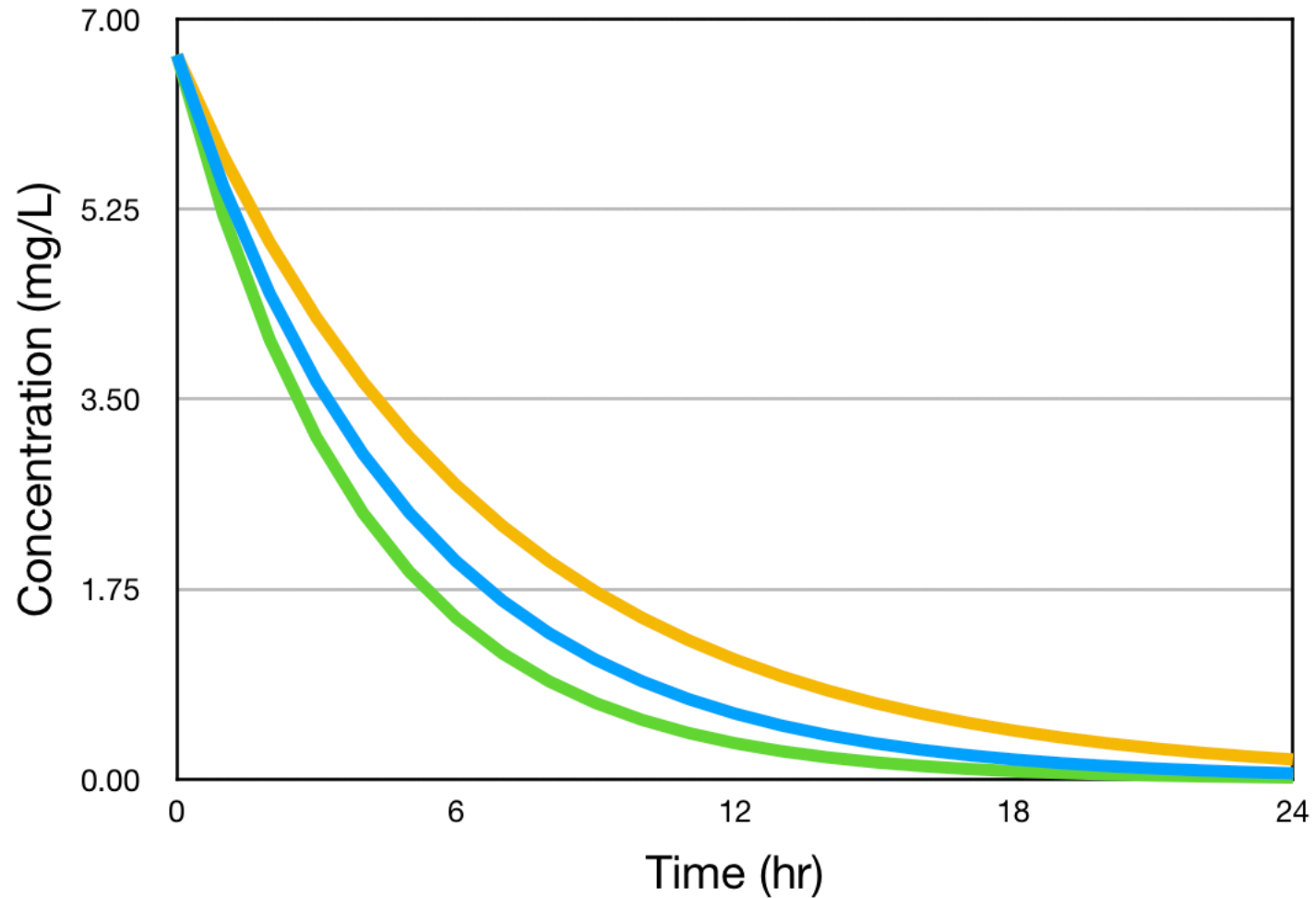
Graphical Approach

Concentration versus Time



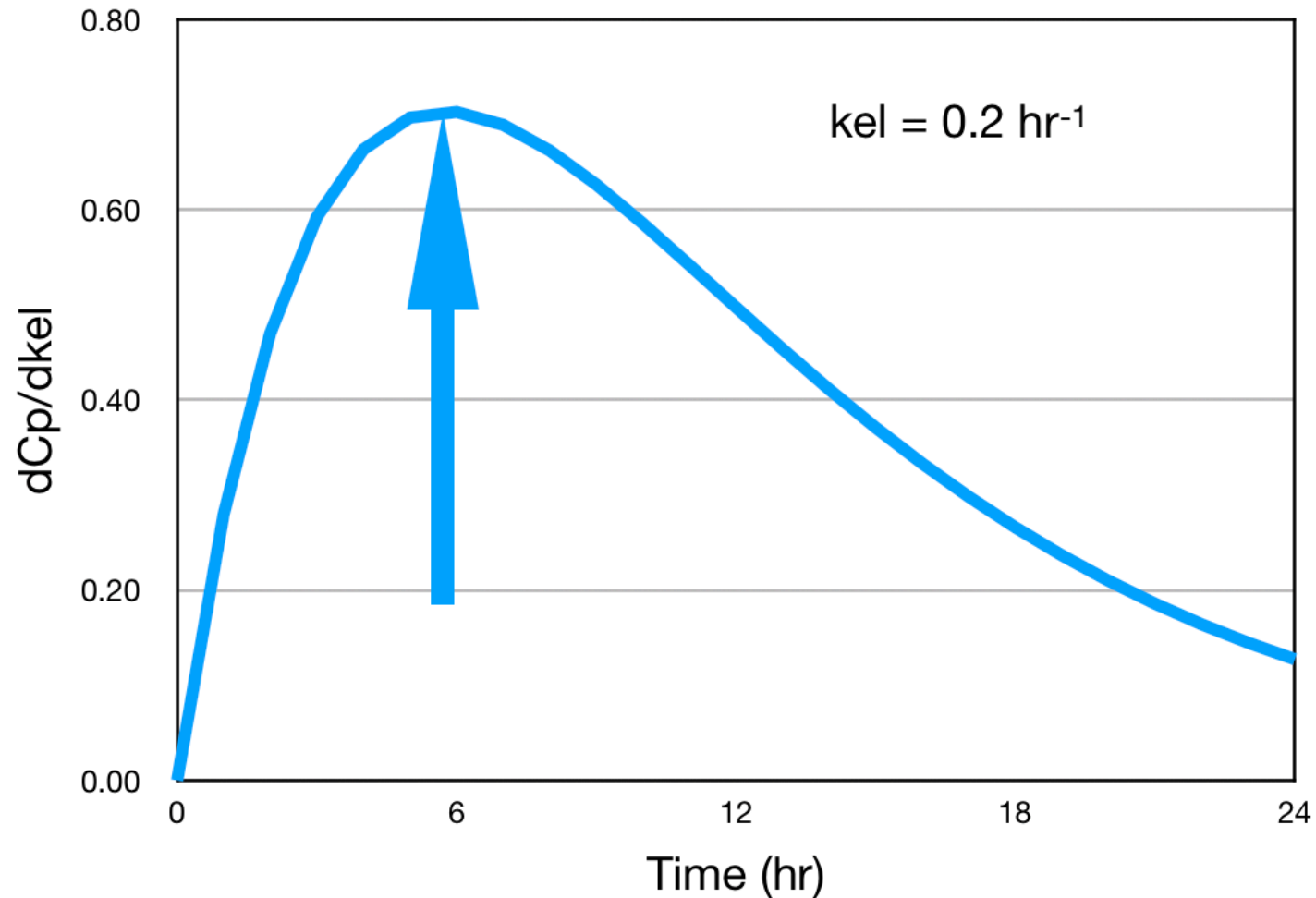
Graphical Approach

Vary k_{el} (with Constant Value of V)



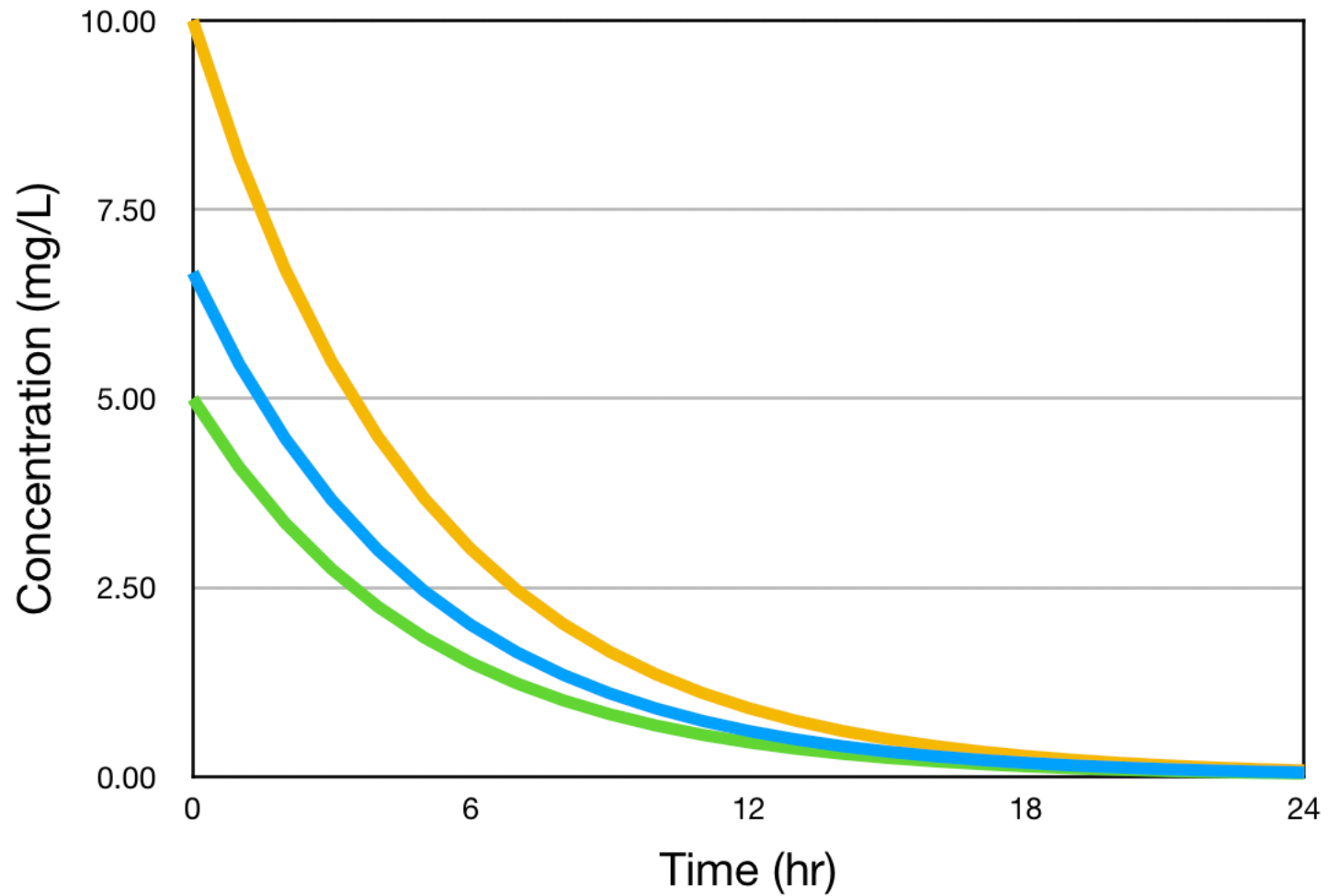
Graphical Approach

Vary k_{el} (with Constant Value of V)



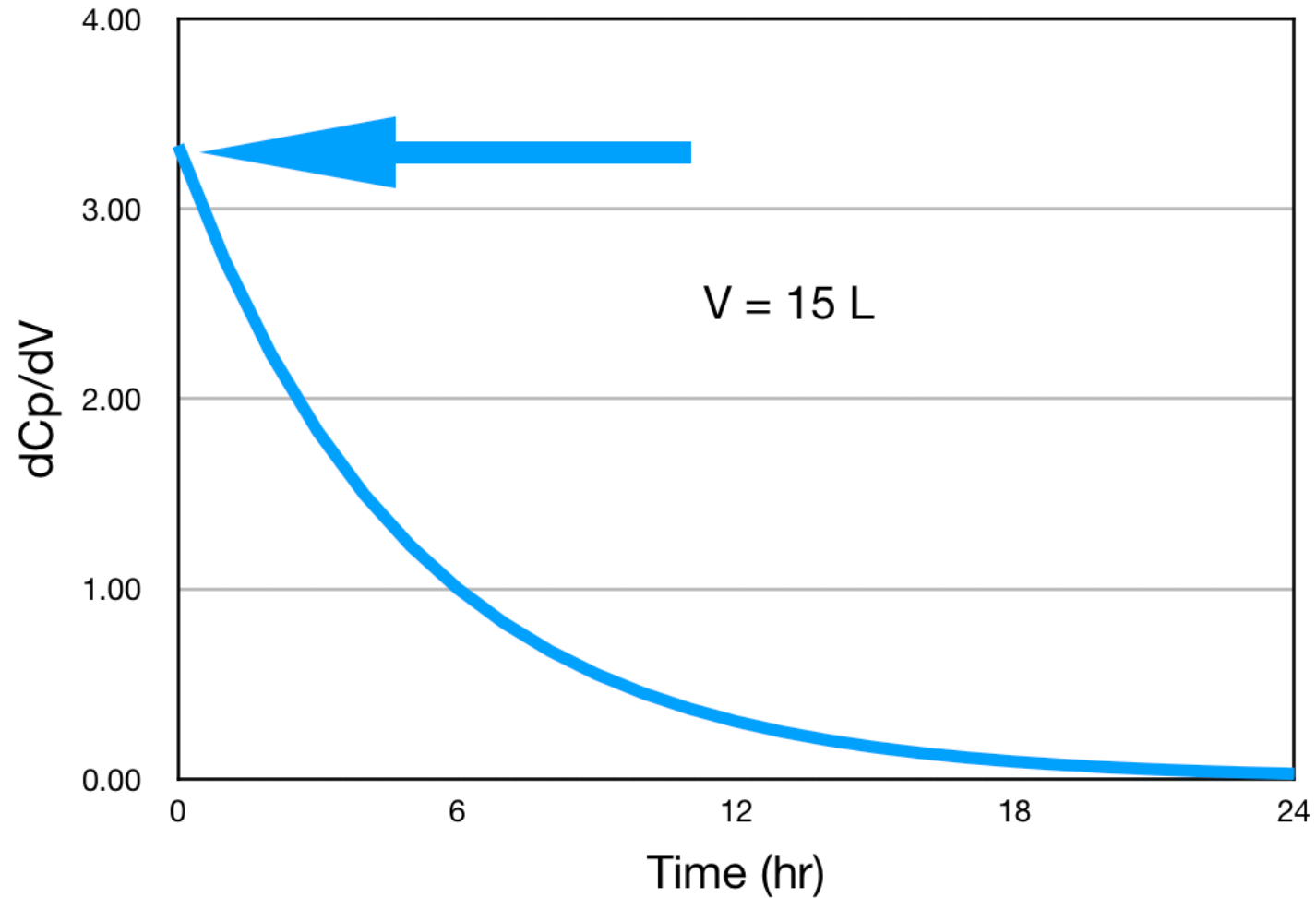
Graphical Approach

Vary V (with Constant Value of k_{el})



Graphical Approach

Vary V (with Constant Value of k_{el})



Analytical Approach

- Differentiate C_p versus Parameter, P_i , to Determine dC_p/dP_i
- Differentiate dC_p/dP_i versus Time to Determine $d^2C_p/dt.P_i$
- Set $d^2C_p/dt.P_i$ equal to 0 to Find the Time for the Maximum Value of dC_p/dP_i
- Solve for Time

Analytical Approach

One Compartment - IV Bolus Dose

$$C_p = \frac{Dose}{V} \cdot e^{-kel \cdot t}$$

$$\frac{dC_p}{dkel} = - \frac{t \cdot Dose}{V} \cdot e^{-kel \cdot t}$$

$$\frac{d^2 C_p}{dkel \cdot dt} = (t \cdot kel - 1) \cdot \frac{Dose}{kel} \cdot e^{-kel \cdot t} = 0$$

$$t = \frac{1}{kel} = \frac{1}{0.2} = 5 \text{ hr}$$

Analytical Approach

One Compartment - IV Bolus Dose

$$C_p = \frac{Dose}{V} \cdot e^{-kel \cdot t}$$

$$\frac{dC_p}{dV} = - \frac{Dose}{V^2} \cdot e^{-kel \cdot t}$$

$$\frac{d^2 C_p}{dV \cdot dt} = \frac{Dose}{V^2 \cdot kel} \cdot e^{-kel \cdot t} = 0$$

$$t \Rightarrow -\infty \text{ hr}$$

Practical Limit $t = 0$

Numerical Approach

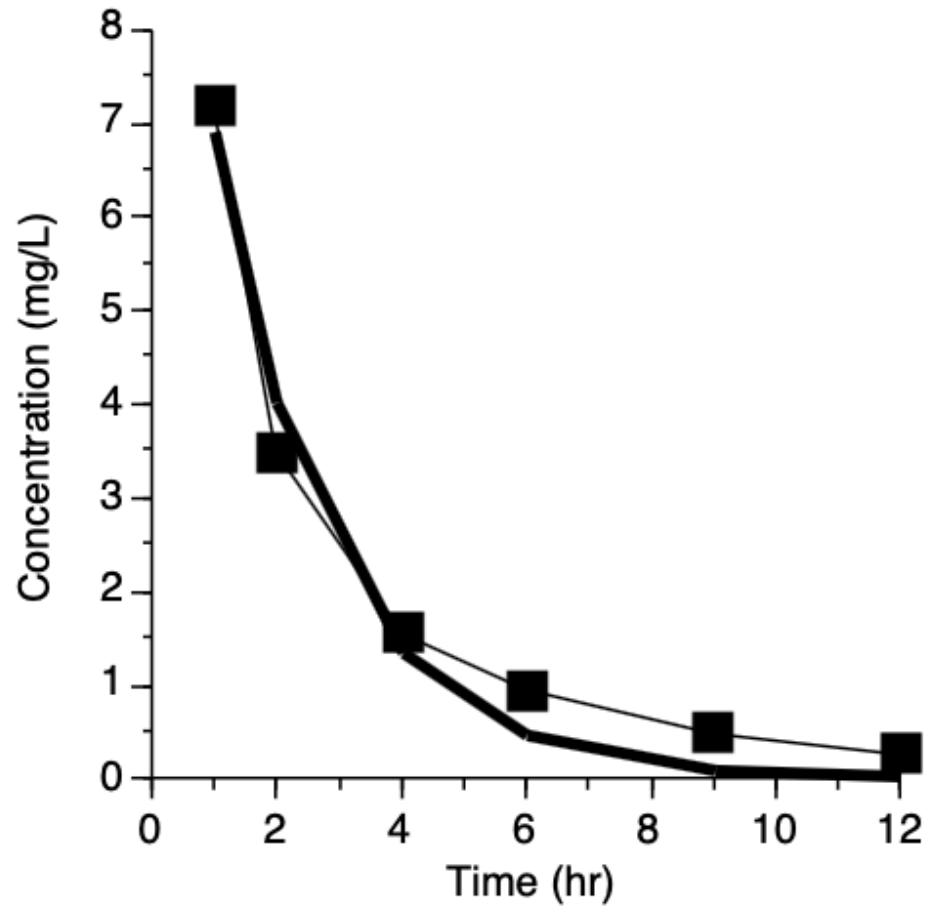
- Use ADAPT II, Sample Module
 - Define the Model
 - Enter the Parameter Values
 - Review Output

Optimal Sampling for Model Selection

- Use the Program DESIGN
- Define both Models
- Run the Program
- Output Gives the Best Time to Distinguish Between Models

DESIGN

- Output Plot



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